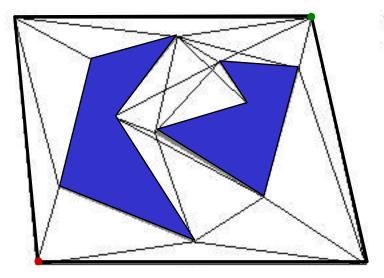
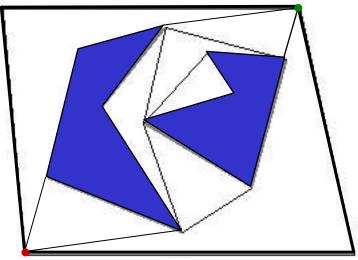
Roadmaps

Vertex Visibility Graph



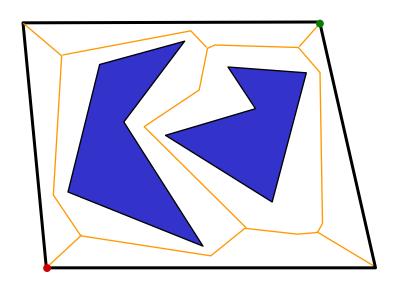
Full visibility graph

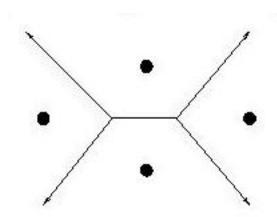


Reduced visibility graph, i.e., not including segments that extend into obstacles on either side.

(but keeping endpoints' roads)

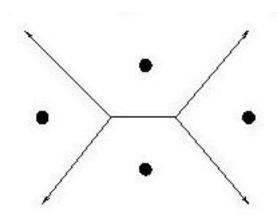
An alternative roadmap





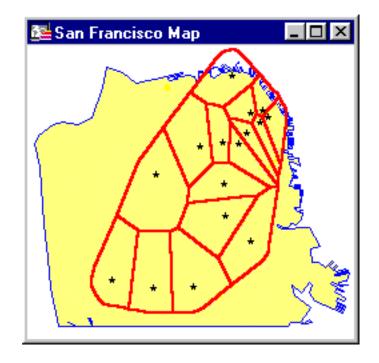
These line segments make up the **Voronoi diagram** for the four points shown here.

Solves the "Post Office Problem"

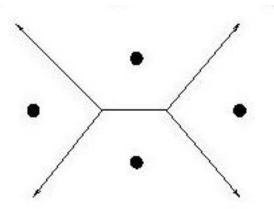


These line segments make up the **Voronoi diagram** for the four points shown here.

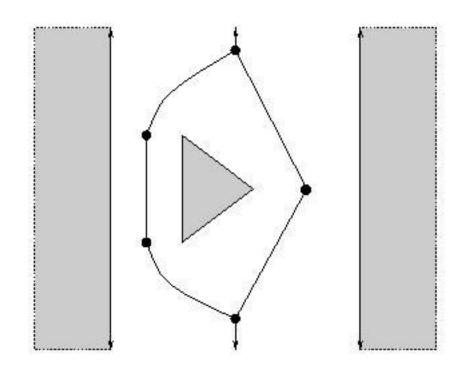
Solves the "Post Office Problem"



or, perhaps, more important problems...



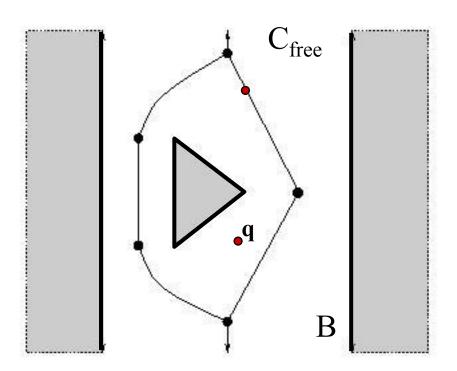
"true" Voronoi diagram (isolates a set of points)



generalized Voronoi diagram What is it?

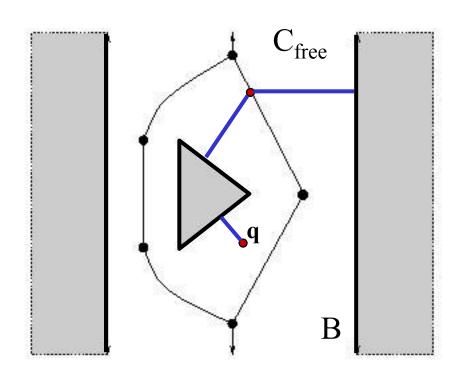
Let B =the boundary of C_{free} .

Let **q** be a point in C_{free} . (•)



Let B =the boundary of C_{free} .

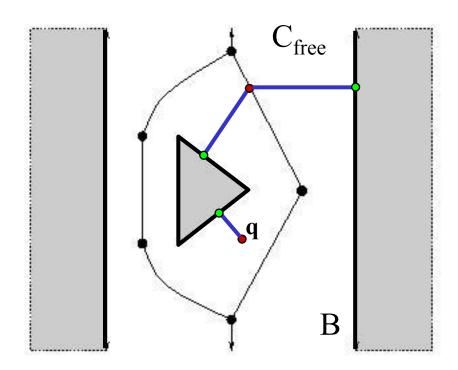
Let \mathbf{q} be a point in C_{free} .



Define *clearance*(q) = min $\{ | q - p | \}$, for all $p \in B$

Let B =the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} .



Define $clearance(q) = min \{ | q - p | \}, for all p \in B$

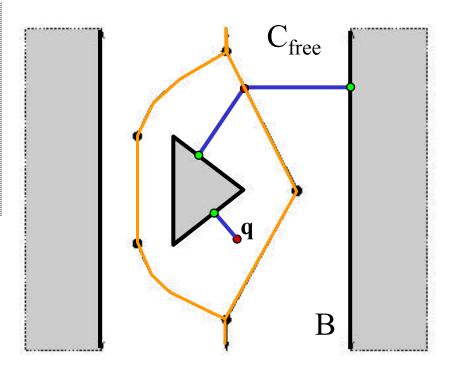
Define $near(q) = \{ p \in B \text{ such that } | q - p | = clearance(q) \}$

Evaluation

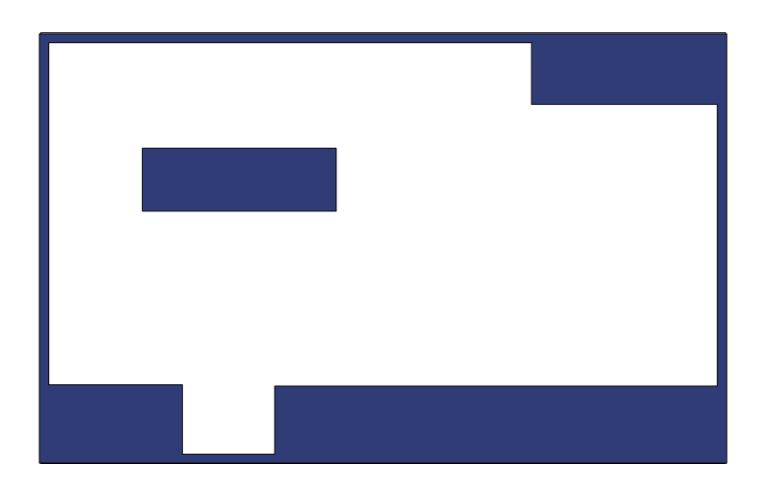
- + maximizes distance from obstacles
- + reduces to graph search
- + can be used in higher-dimensions
- nonoptimal
- real diagrams tend to be noisy

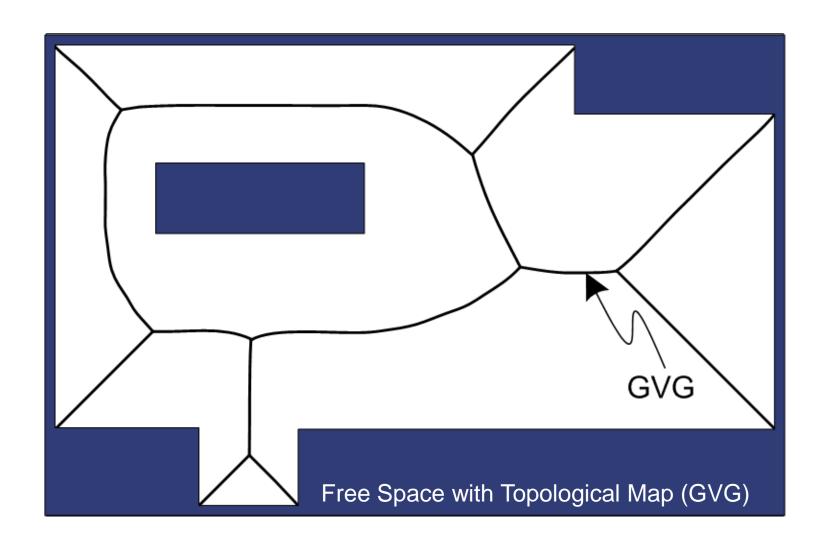
Let B =the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} .

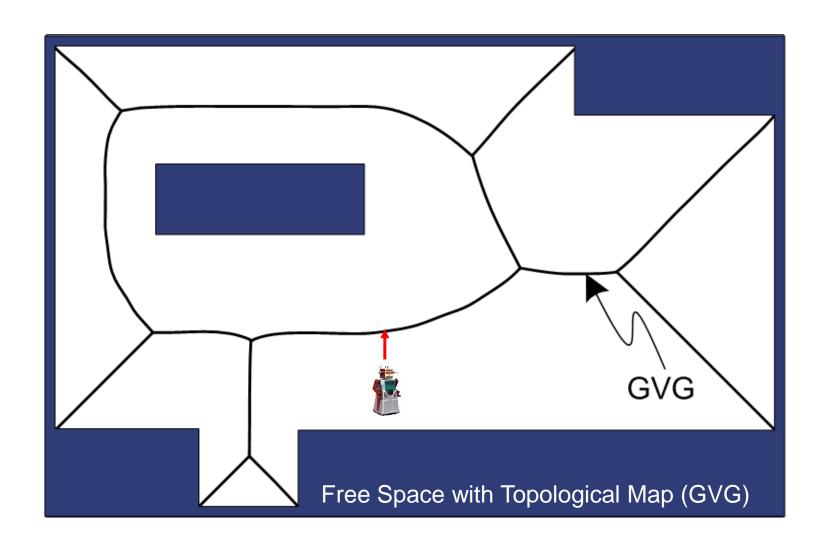


Define
$$clearance(q) = min \{ | q - p | \}$$
, for all $p \in B$
Define $near(q) = \{ p \in B \text{ such that } | q - p | = clearance(q) \}$
 $q \text{ is in the } Voronoi \ diagram \ of \ C_{free} \ if \ | near(q) | > 1$

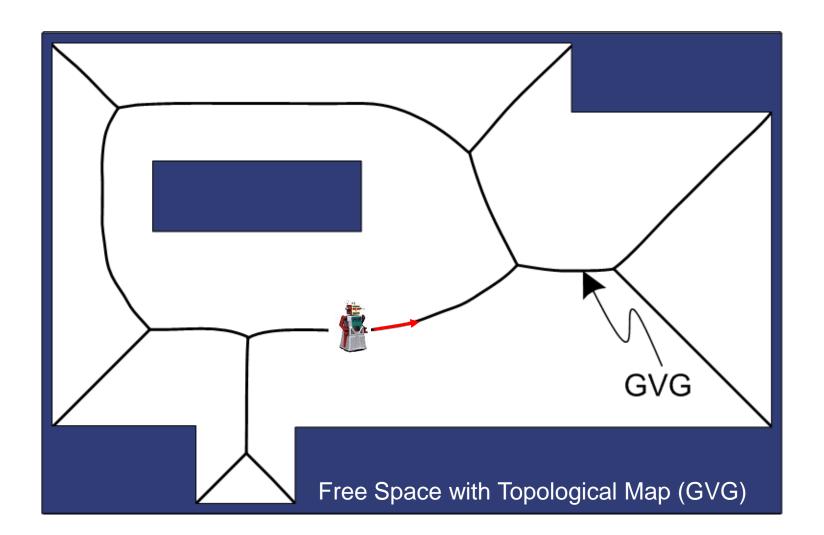




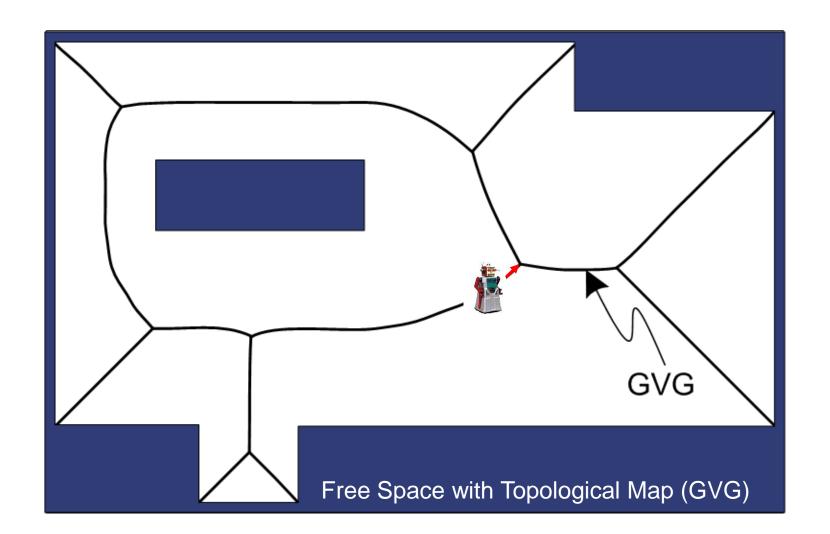
Access GVG



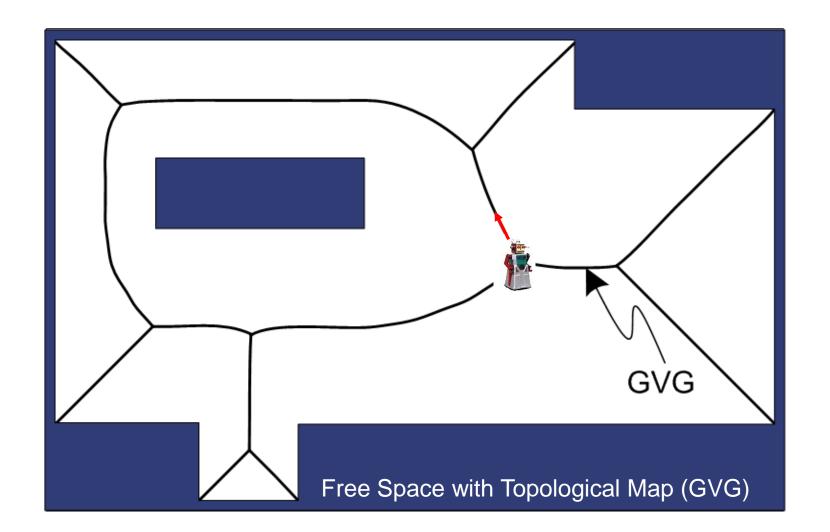
- Access GVG
- •Follow Edge



- •Access GVG •Home to the MeetPoint
- •Follow Edge



- •Access GVG •Home to the MeetPoint
- •Follow Edge •Select Edge

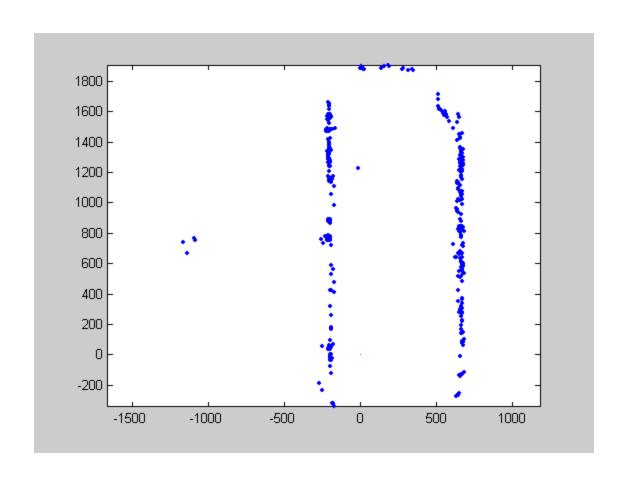


GVG construction using sonar

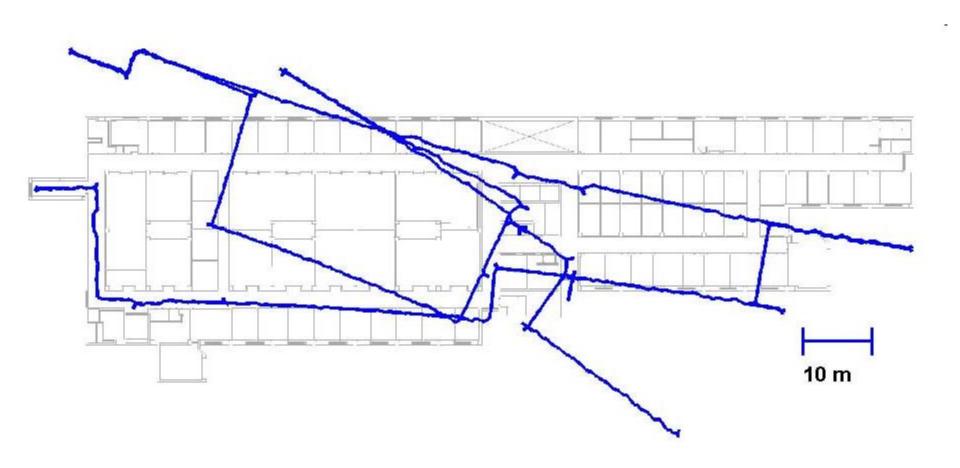


- Nomadic Scout
- Sonar (GVG navigation)
- Camera with omni-directional mirror (feature detection)
- Onboard 1.2 GHz processor

GVG construction using sonar



GVG construction using sonar

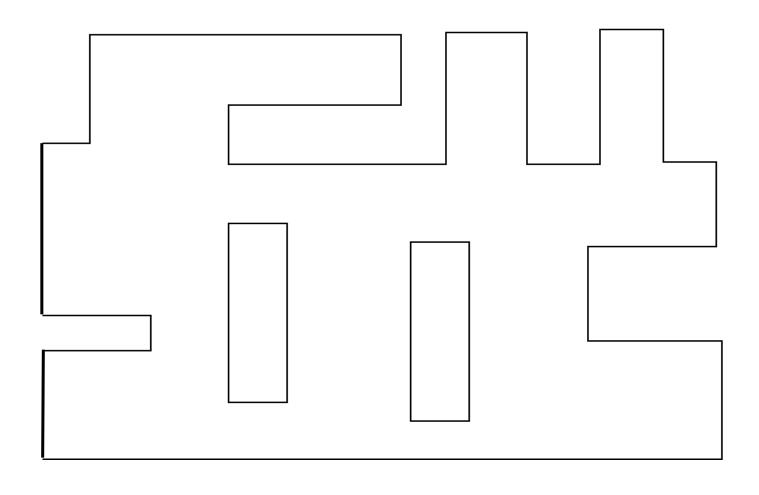


Slammer in Action

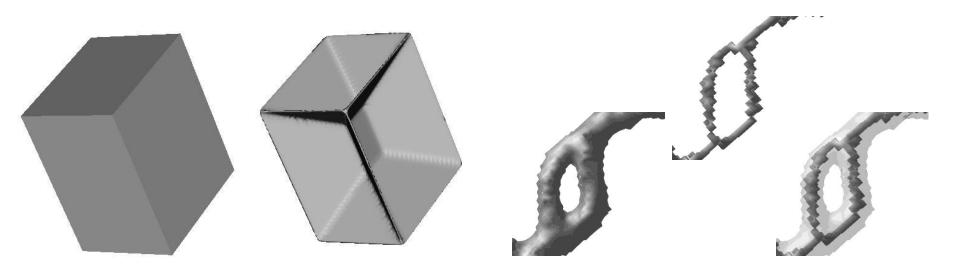




What is the Voronoi Graph?



Voronoi applications

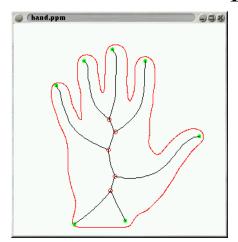


A retraction of a 3d object == "medial surface"

what?

Skeletonizations resulting from constant-speed curve evolution

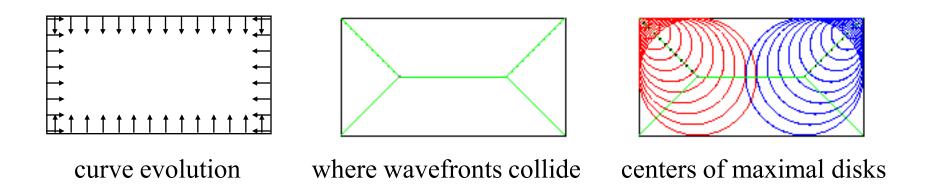






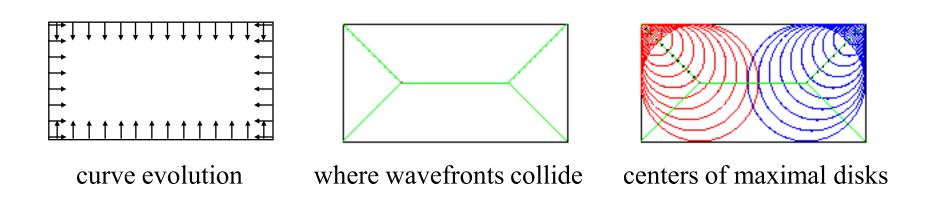
in 2d, it's called a *medial axis*

skeleton → shape



again reduces a 2d (or higher) problem to a question about graphs...

skeleton → shape

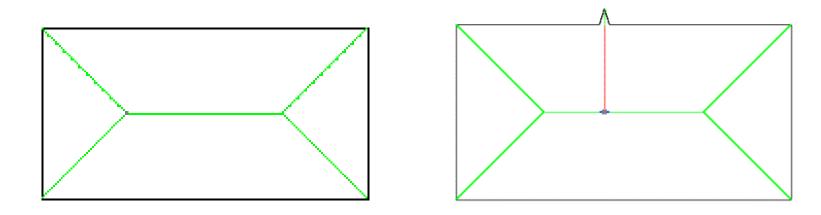


again reduces a 2d (or higher) problem to a question about graphs...



graph matching

Problems

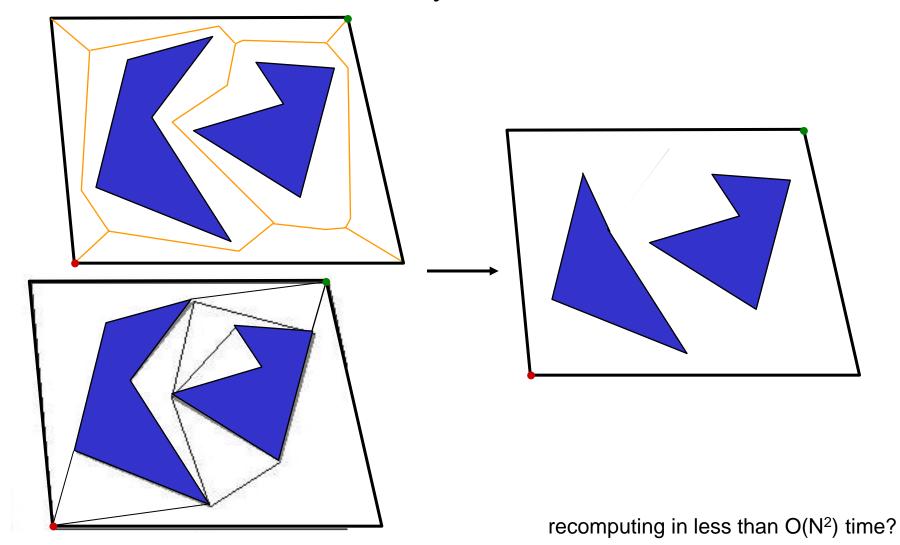


The skeleton is sensitive to small changes in the object's boundary.

- graph isomorphism (and lots of other graph questions) : NP-complete

Roadmap problems

If an obstacle decides to roll away... (or wasn't there to begin with)



Experiments at CSA

• Autonomous Over-the-Horizon Navigation



CSA Experiments



CSA Experiments



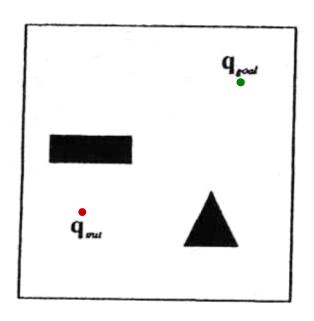
Practical Considerations

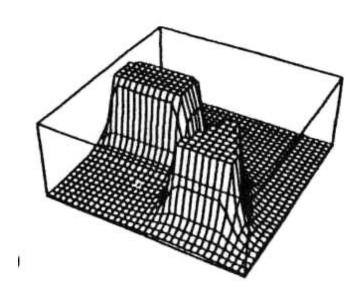


Path Planning

Potential Field methods

• compute a repulsive force away from obstacles

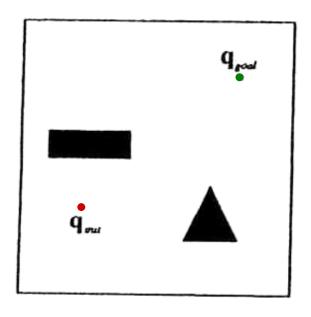


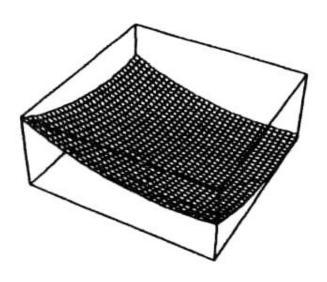


Local techniques

Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal

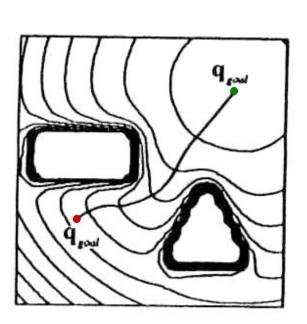


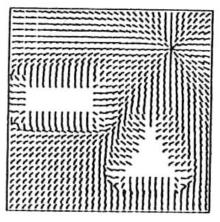


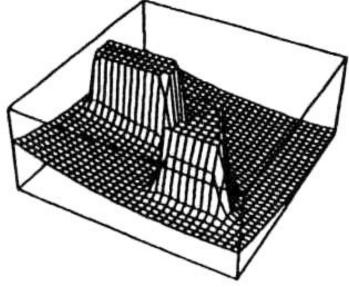
Local techniques

Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal
- → let the sum of the forces control the robot



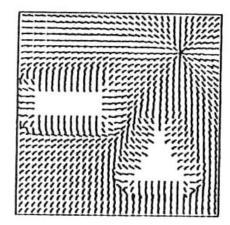


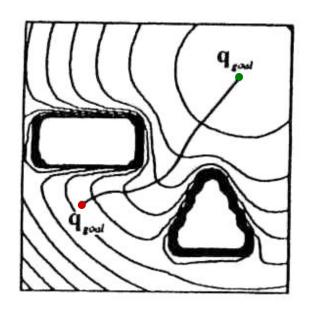


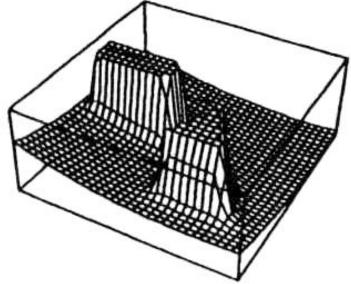
Local techniques

Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal
- → let the sum of the forces control the robot

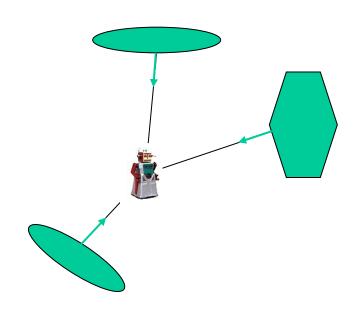






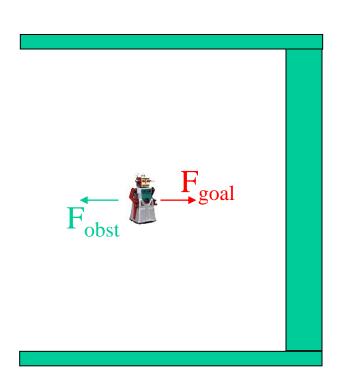
To a large extent, this is computable from sensor readings

Sensor Based Calculations



Major Problem?

Local Minima!



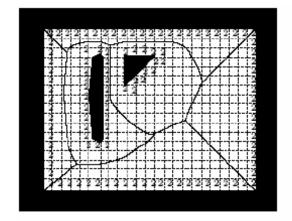


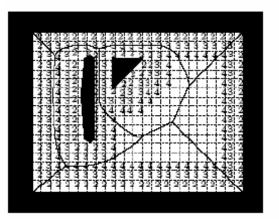
Simulated Annealing

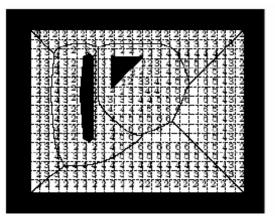
• Every so often add some random force

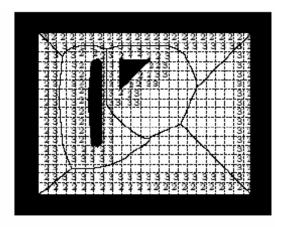
Known Map

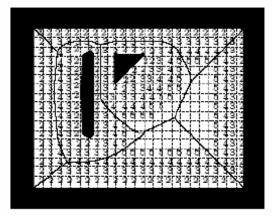
Brushfire Transform

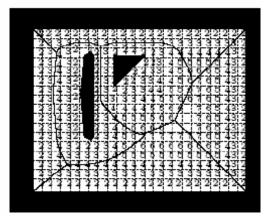




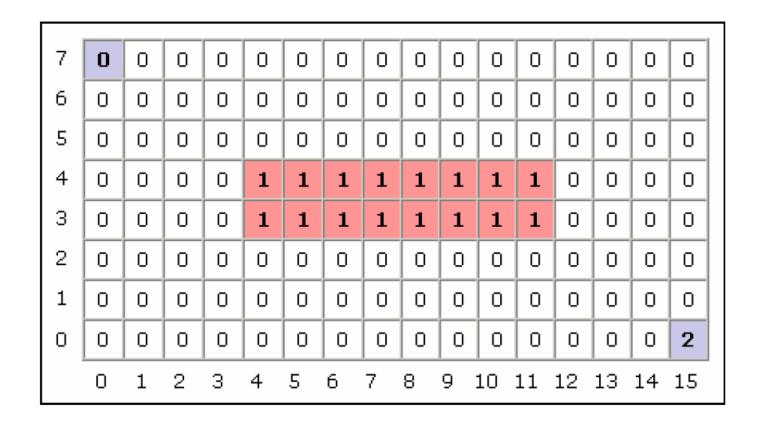






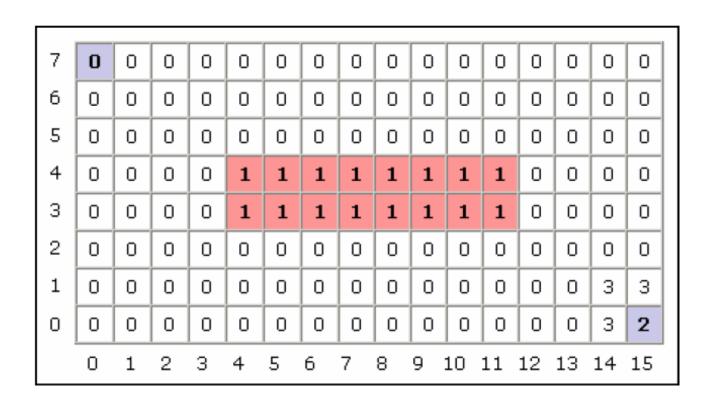


The Wavefront Planner: Setup



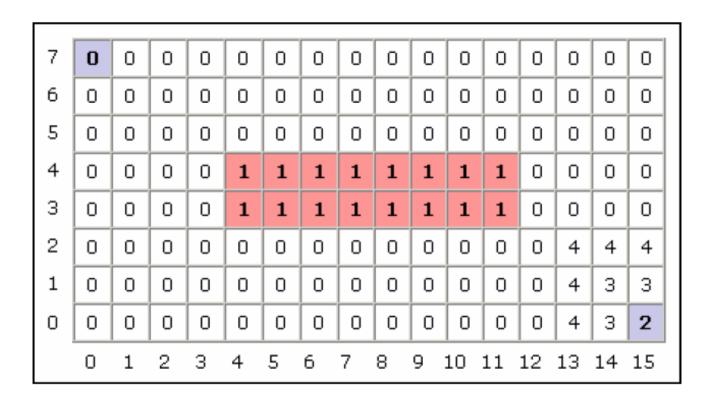
The Wavefront in Action (Part 1)

- Starting with the goal, set all adjacent cells with "0" to the current cell + 1
 - 4-Point Connectivity or 8-Point Connectivity?
 - Your Choice. We'll use 8-Point Connectivity in our example



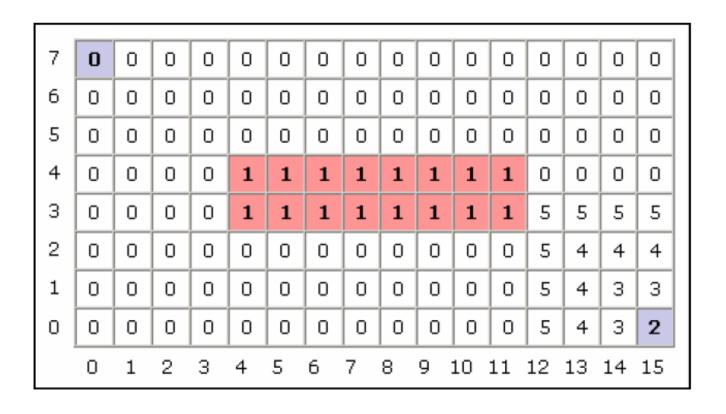
The Wavefront in Action (Part 2)

- Now repeat with the modified cells
 - This will be repeated until no 0's are adjacent to cells with values ≥ 2
- 0's will only remain when regions are unreachable



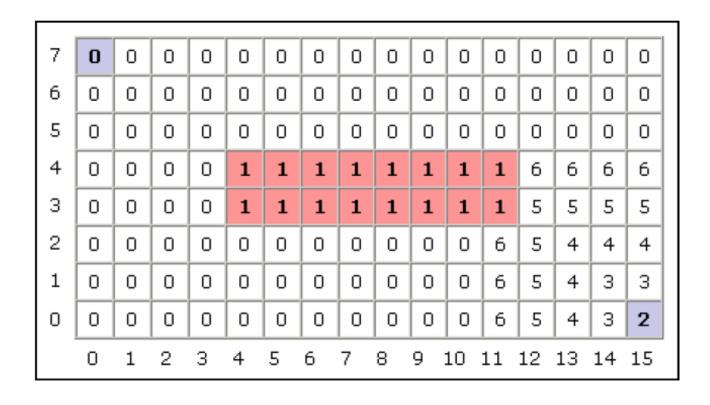
The Wavefront in Action (Part 3)

• Repeat



The Wavefront in Action (Part 3)

• Repeat



The Wavefront in Action (Part 3)

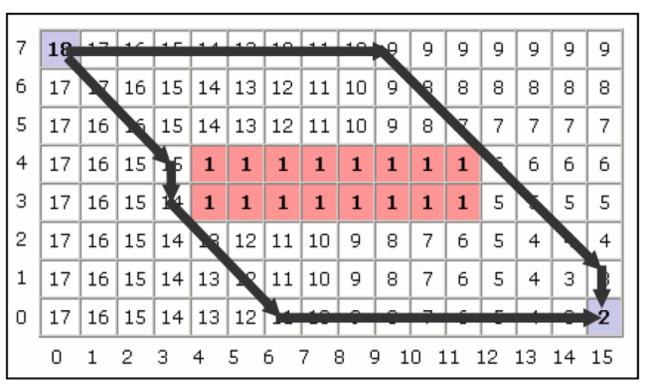
Until Done

- 0's would only remain in the unreachable areas

7	18	17	16	15	14	13	12	11	10	9	9	9	9	9	9	9
6	17	17	16	15	14	13	12	11	10	9	8	8	8	8	8	8
5	17	16	16	15	14	13	12	11	10	9	8	7	7	7	7	7
4	17	16	15	15	1	1	1	1	1	1	1	1	6	6	6	6
3	17	16	15	14	1	1	1	1	1	1	1	1	5	5	5	5
2	17	16	15	14	13	12	11	10	9	8	7	6	5	4	4	4
1	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	3
0	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2
	0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15															

The Wavefront in Action

- To find the shortest path, according to your metric, simply always move toward a cell with a lower number
 - The numbers generated by the Wavefront planner are roughly proportional to their distance from the goal



Two possible shortest paths shown

Introduction to Mapping

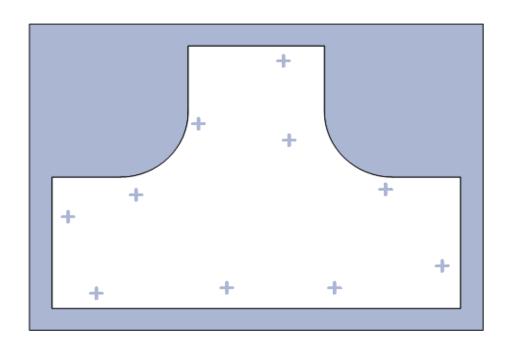
- What the world looks like?
- Knowledge representation
 - Robotics, AI, Vision
- Who is the end-user?
 - Human or Machine
- Ease of Path Planning
- Uncertainty!

Simultaneous Localization And Mapping

SLAM is the process of building a map of an environment while, at the same time, using that map to maintain the location of the robot.

- Problems for SLAM in large scale environments:
 - Controlling growth of uncertainty and complexity
 - Achieving autonomous exploration

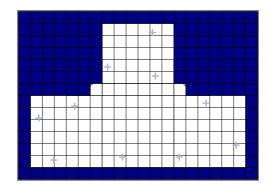
Consider this Environment:

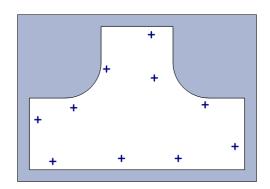


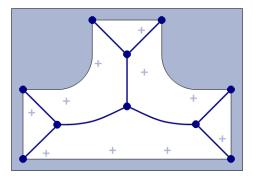
Three Basic Map Types

Topological:

Collection of nodes and their interconnections







Three Basic Map Types

	Grid-Based	Feature-Based	Topological	
Construction	Occupancy grids	Kalman Filter	Navigation control laws	
Complexity	Grid size <i>and</i> resolution	Landmark covariance (N ³)	Minimal complexity	
Obstacles	Discretized obstacles	Only structured obstacles	GVG defined by the safest path	
Localization	Discrete localization	Arbitrary localization	Localize to nodes	
Exploration	Frontier-based exploration	No inherent exploration	Graph exploration	

Other Maps

	Appearance	Geometry	Mesh
	Based	Based	Based
Construction	Images	Lines, planes, etc	Mesh
Path Planning	N/A	Geometry based	Graph based
Localization	Arbitrary localization	Arbitrary localization	Arbitrary localization